# Planning to Chronicle 

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#### Abstract

An important class of applications entails a robot monitoring, scrutinizing, or recording the evolution of an uncertain timeextended process. This sort of situation leads to an interesting family of planning problems in which the robot is limited in what it sees and must, thus, choose what to pay attention to. The distinguishing characteristic of this setting is that the robot has influence over what it captures via its sensors, but exercises no causal authority over the evolving process. As such, the robot's objective is to observe the underlying process and to produce a 'chronicle' of occurrent events, subject to a goal specification of the sorts of event sequences that may be of interest. This paper examines variants of such problems when the robot aims to collect sets of observations to meet a rich specification of their sequential structure. We study this class of problems by modeling a stochastic process via a variant of a hidden Markov model, and specify the event sequences of interest as a regular language, developing a vocabulary of 'mutators' that enable sophisticated requirements to be expressed. Under different suppositions about the information gleaned about the event model, we formulate and solve different planning problems. The core underlying idea is the construction of a product between the event model and a specification automaton. The paper reports and compares performance metrics by drawing on some small case studies analyzed in depth in simulation.


Keywords: Planning, Story-telling, Reconnoitering, Raconteuring

## 1 Motivation and Introduction

This paper is about robotic planning problems in which the goals are expressed as time-extended sequences of discrete events whose occurrence the robot cannot causally influence. As a concrete motivation for this sort of setting, consider the proliferation of home videos. These videos are, with remarkably few exceptions, crummy specimens of the cinematic arts. They fail, generally, to establish and then bracket a scene; they often founder in emphasizing the importance of key subjects within the developing action, and are usually unsuccessful in attempts to trace an evolving narrative arc. And the current generation of autonomous

[^0]personal robots and video drones, in their roles as costly and glorified 'selfie sticks,' are set to follow suit. The trouble is that capturing footage to tell a story is challenging. A camera can only record what you point it toward, so part of the difficulty stems from the fact that you can't know exactly how the scene will unfold before it actually does. Moreover, what constitutes structure isn't easily summed up with a few trite quantities. Another part of the challenge, of course, is that one has only limited time to capture video footage.

Setting aside pure vanity as a motivator, many applications can be cast as the problem of producing a finite-length sensor-based recording of the evolution of some process. As the video example emphasizes, one might be interested in recordings that meet rich specifications of the event sequences that are of interest. When the evolution of the event-generating process is uncertain/nondeterministic and sensing is local (necessitating its active direction), then one encounters an instance from this class of problem. The broad class encompasses many monitoring and surveillance scenarios. An important characteristic of such settings is that the robot has influence over what it captures via its sensors, but cannot control the process of interest.

Our incursion into this class of problem involves two lines of attack. The first is a wide-embracing formulation in which we pose a general stochastic model, including aspects of hidden/latent state, simultaneity of event occurrence, and various assumptions on the form of observability. Secondly, we specify the sequences of interest via a deterministic finite automaton (DFA), and we define several language mutators, which permit composition and refinement of specification DFAs, allowing for rich descriptions of desirable event sequences. The two parts are brought together via our approach to planning: we show how to compute an optimal policy (to satisfy the specifications as quickly as possible) via a form of product automaton. Empirical evidence from simulation experiments attests to the feasibility of this approach.

Beyond the pragmatics of planning, a theoretical contribution of the paper is to prove a result on representation independence of the specifications. That is, though multiple distinct DFAs may express the same regular language and despite the DFA being involved directly in constructing the product automaton used to solve the planning problem, we show that it is merely the language expressed that affects the resulting optimal solution. Returning to mutators that transform DFAs, enabling easy expression of sophisticated requirements, we distinguish when mutators preserve representational independence too.

## 2 Related Work

Our interest in understanding robot behavior in terms of the robots' observations of a sequence of discrete events is, of course, not unique. The story validation problem $[24,25]$ can be viewed as an inverse of our problem. The aim there is to determine whether a given story is consistent with a sequence of events captured by a network of sensors in the environment. In our problem, it is the robot that needs to capture a sequence of events that constitute a desired story.

Video summarization is the problem of making a 'good' summary of a given video by prioritizing sequences of frames based on some selection criterion (im-
portance, representativeness, diversity, etc.). Various approaches include identifying important objects [8], finding interesting events [4], selection using supervised learning [3], and finding inter-frame connections [10]. For a survey on video summarization see [23], which one might augment with the more recent results of $[5,11,12,26]$. Girdhar and Dudek [2] considered the related vacation snapshot problem, in which the goal is to retain a diverse subset from data observed by a mobile robot. However, in such summarization techniques, the problem is essentially to post-process a collection of images already recorded. This paper, by contrast, addresses the problem of deciding which video segments the robot should attempt to capture in the first place.

For text-based and interactive narratives, a variety of methods are known for narrative planning and generating natural language stories $[15,16]$.

Closely related research to the present paper is [21], which introduces the idea of using a team of autonomous robots, coordinated by a planner, to capture a sequence of events specifying a given narrative structure. That work raised (but did not answer) several questions, among which is how the robot can formulate effective plans to capture events relevant to the story specification. Here we build upon that prior effort showing how such plans can be formed in a principled way.

Related to our problem are also the theories of Markov decision processes (MDPs) and partially observable Markov decision processes (POMDPs), which are surveyed in $[1,7,17,20]$. We solve our problem by constructing a product of the event model and the specification, which together yield a specific POMDP.

## 3 The Problem

First, we introduce the basic elements of our model and problem formalization.

### 3.1 Events and observations

The essential objects of interest are events, that is, atomic occurrences situated at specific times and places. We propose to treat each event as a letter drawn from a finite alphabet $E$, a set which contains all possible events. Accordingly, any finite sequence of events, in particular a story $\xi$ the robot wants to record from the events that occur in the system, is a finite word in $E^{*}$.

We model the occurrence of events using a structure defined as follows.
Definition 1 (event model). An event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$ is a tuple in which (1) $S$, which is a nonempty finite set, is the state space of the model; (2) $\mathbf{P}: S \times S \rightarrow[0,1]$ is the transition probability function of the model, such that for each state $s \in S, \sum_{s^{\prime} \in S} \mathbf{P}\left(s, s^{\prime}\right)=1$; (3) $s_{0} \in S$ is the initial state; (4) $E$ is the set of all possible events; and (5) $g: S \rightarrow 2^{E}$ is a labeling function assigning, to each state, the (possibly empty) set of events that are occurring (mnemonically, 'going-on') simultaneously at that state. We assume that $g\left(s_{0}\right)=\varnothing$.
An execution of the model starts from the initial state $s_{0}$ and then, at each time step $k$, the system makes a transition from state $s_{k}$ to state $s_{k+1}$, the latter being chosen randomly based on $\mathbf{P}$ from those states for which $\mathbf{P}\left(s_{k}, \cdot\right)>0$. This execution specifies a path $s_{0} s_{1} \cdots$. For every time step $k$, when the system enters state $s_{k}$, each event in $g\left(s_{k}\right)$ occurs simultaneously.

We are interested in scenarios in which a robot is tasked with recording certain sequences of events. We model the state of the event model as only partially observable to the robot. That is, the current state $s_{k}$ of the event model is hidden from the robot, but the system instead emits an output observable to the robot at each time step. The next definition formalizes the idea.

Definition 2 (observation model). For a given event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}\right.$, $E, g)$, an observation model $\mathcal{B}=(Y, h)$ is a pair in which (1) $Y$ is a set of observations or outputs; (2) $h: S \times Y \rightarrow[0,1]$ is the emission probability function of the model, such that for each state $s \in S, \sum_{y \in Y} h(s, y)=1$.

At each time step, when the system enters a state $s_{k}$, it emits an output $y_{k}$, drawn according to $h\left(s_{k}, \cdot\right)$. The emitted output $y_{k}$ is observable to the robot. An event model and observation model can be depicted together as a directed graph (e.g., see Figure 1a), where we show each state's events as an attached set (in braces in the figure) and display observations from $Y$ along with their emission probabilities (in brackets). We consider, as important special cases, two particular types of observation models.
Definition 3. Given an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$ with observation model $\mathcal{B}=(Y, h)$, we say that $\mathcal{B}$ makes $\mathcal{M}$ fully observable if (1) $Y=S$, and (2) $h(s, y)=$ 1 if and only if $s=y$.
We write $\mathcal{B}_{\text {obs }}(\mathcal{M})$ to denote the unique observation model that makes $\mathcal{M}$ fully observable. At the other extreme, another special event model is one in which the emitted outputs do not help at all to reduce uncertainty.
Definition 4. Given an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$ with observation model $\mathcal{B}=(Y, h)$, then $\mathcal{B}$ causes the event model to be fully hidden if the observation space $Y$ is a singleton set.
Since the particular single observation comprising $Y$ is unimportant, by $\mathcal{B}_{\text {hid }}(\mathcal{M})$ we denote some observation model making $\mathcal{M}$ fully hidden.

### 3.2 Story specifications, belief states, and policies

As the system evolves along $s_{0} s_{1} s_{2} \cdots$, the robot attempts to record some of the events that actually occur in the world to form a story $\xi \in E^{*}$. We specify the desired story using a deterministic finite automaton (DFA) $\mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$, where $Q$ is its state space, $E$ is its alphabet, $\delta: Q \times E \rightarrow Q$ is its transition function, $q_{0}$ its initial state, and $F \subseteq Q$ is the set of all final (accepting) states of the automaton. In other words, we want the robot to make a story $\xi$ in the language of $\mathcal{D}$, denoted $\mathcal{L}(\mathcal{D})$, which is the set of all strings in $E^{*}$ that when are tracked from $q_{0}$, the automaton reaches an accepting state.

The semantics of event capture are as follows. At each step $k \geq 0$, the robot chooses one event $e$ from $E$ to attempt to record in the next step, $k+1$. If any of the actual events that do happen at step $k+1$ (i.e., any of the events in $g\left(s_{k+1}\right)$ ) match the robot's prediction, then the robot successfully records this event; otherwise, it records nothing. The robot is aware of the success or failure of each of its attempts. The robot stops making guesses and observations once it has recorded a desired story - a story in $\mathcal{L}(\mathcal{D})$.

To estimate the current state, the robot maintains, at each time step $k$, a belief state $b_{k}: S \rightarrow[0,1]$, in which $\sum_{s \in S} b_{k}(s)=1$. For each $s \in S, b_{k}(s)$ represents the probability that the event model is in state $s$ at time step $k$, according to the information available to the robot, including both the observations emitted directly by the event model, along with the sequence of successes or failures in recording events. It also maintains, for each time $k$, the sequence $\xi_{k}$ of events it has recorded until time step $k$, and the (unique) DFA state $q_{k}$ obtained by $\xi_{k}$.

The robot's predictions are governed by a policy $\pi: \Delta(S) \times Q \rightarrow E$ that depends on the belief state and the state of the DFA. At time step $k+1$, the robot may append a recorded event to $\xi_{k}$ via the following formula:

$$
\xi_{k+1}= \begin{cases}\xi_{k} \pi\left(b_{k}, q_{k}\right) & \pi\left(b_{k}, q_{k}\right) \in g\left(s_{k+1}\right)  \tag{1}\\ \xi_{k} & \pi\left(b_{k}, q_{k}\right) \notin g\left(s_{k+1}\right)\end{cases}
$$

The initial condition is that $\xi_{0}=\epsilon$, in which $\epsilon$ is the empty string. The robot changes the value of variable $q_{k}$ only when the guessed event actually happened:

$$
q_{k+1}= \begin{cases}\delta\left(q_{k}, \pi\left(b_{k}, q_{k}\right)\right) & \pi\left(b_{k}, q_{k}\right) \in g\left(s_{k+1}\right)  \tag{2}\\ q_{k} & \pi\left(b_{k}, q_{k}\right) \notin g\left(s_{k+1}\right)\end{cases}
$$

The robot stops when $q_{k} \in F$.

### 3.3 Optimal recording problems

The robot's goal is to record a story (or video) as quickly as possible. We consider this problem in three different settings: a general setting without any restriction on the event model, a setting in which the event model is fully observable, and a final one in which the event model is fully hidden. First, the general setting.

## Problem: Recording Time Minimization (Rtm)

Input: An event set $E$, an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$ with observation model $\mathcal{B}=(Y, h)$, and a DFA $\mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$.
Output: A policy minimizing the expected number of steps $k$ until $\xi_{k} \in \mathcal{L}(\mathcal{D})$.
Note that $k$ is not necessarily the length of the resulting story $\xi_{k}$, but rather is the number of steps the system runs to capture that story. In fact, $\left|\xi_{k}\right| \leq k$.

The second setting constrains the system to be fully observable.
Problem: RTM with Fully Observable Model (Rтм/Fom)
Input: An event set $E$, an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$, and a DFA $\mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$.
Output: A policy that, under observation model $\mathcal{B}_{\text {obs }}(\mathcal{M})$, minimizes the expected number of steps $k$ until $\xi_{k} \in \mathcal{L}(\mathcal{D})$.

In this setting, because states are fully observable to the robot, we might have defined the policy as a function over $S \times Q$ rather than over $\Delta(S) \times Q$. Nonetheless, our current definition does not pose any problem. Any reachable belief state in this setting considers only a single outcome (i.e., given any $k$, $b_{k}(s)=1$ for exactly one $s \in S$ ) and thus, we are interested in the optimal policy only for those reachable beliefs.

The third setting assumes a fully hidden event model state.

Problem: RTM with Fully Hidden Model (Rtm/Fнм)
Input: An event set $E$, an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$, and a DFA $\mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$.
Output: A policy that, under observation model $\mathcal{B}_{\text {hid }}(\mathcal{M})$, minimizes the expected number of steps $k$ until $\xi_{k} \in \mathcal{L}(\mathcal{D})$.

## 4 Algorithm Description

Next we give an algorithm for Rtm, which also solves Rtm/Fom and RTm/Fhm, which are basically the same RTM problem but with two special kinds of event models as inputs to the problem.

### 4.1 The Goal POMDP

The first step of the algorithm constructs a specific partially observable Markov decision process (POMDP), which we term the Goal POMDP, as follows:
Definition 5 (Goal POMDP). For an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$ with observation model $\mathcal{B}=(Y, h)$, and a $D F A \mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$, the associated Goal POMDP is a tuple $\mathcal{P}_{(\mathcal{M}, \mathcal{B} ; \mathcal{D})}=\left(X, A, b_{0}, \mathbf{T}, X_{G}, Z, \mathbf{O}, c\right)$, in which

1. $X=S \times Q$ is the state space;
2. $A=E$ is the action space;
3. $b_{0} \in \Delta(X)$ is the initial belief state, in which $b_{0}(x)=1$ iff $x=\left(s_{0}, q_{0}\right)$;
4. $\mathbf{T}: X \times A \times X \rightarrow[0,1]$ is the transition probability function such that for each $e \in E$ and $(s, q),\left(s^{\prime}, q^{\prime}\right) \in X$,

$$
\mathbf{T}\left((s, q), e,\left(s^{\prime}, q^{\prime}\right)\right)= \begin{cases}\mathbf{P}\left(s, s^{\prime}\right) & \text { if } q \notin F, q^{\prime}=\delta(q, e), \text { and } e \in g\left(s^{\prime}\right)  \tag{4.a}\\ \mathbf{P}\left(s, s^{\prime}\right) & \text { if } q \notin F, q^{\prime}=q, \text { and } e \notin g\left(s^{\prime}\right) \\ 1 & \text { if } q \in F, q^{\prime}=q, \text { and } s=s^{\prime} \\ 0 & \text { otherwise; }\end{cases}
$$

5. $X_{G}=S \times F$ is the set of goal states;
6. $Z=(\{$ True, False $\} \times Y) \cup\{\perp\}$ is the set of observations;
7. $\mathbf{O}: A \times X \times Z \rightarrow[0,1]$ is the observation probability function such that for each $e \in E, s \in S, q \in Q$, and $y \in Y$ :
(a) $\mathbf{O}(e,(s, q)$, (True, $y))=h(s, y)$ if $q \notin F$ and $e \in g(s)$,
(b) $\mathbf{O}(e,(s, q),($ False, $y))=0$ if $q \notin F$ and $e \in g(s)$,
(c) $\mathbf{O}(e,(s, q),($ False, $y))=h(s, y)$ if $q \notin F$ and $e \notin g(s)$,
(d) $\mathbf{O}(e,(s, q)$, (True, $y))=0$ if $q \notin F$ and $e \notin g(s)$,
(e) $\mathbf{O}(e,(s, q), \perp)=1$ if $q \in F$;
8. $c: X \times A \rightarrow \mathbb{R}_{\geq 0}$ is the cost function such that for each $x \in X$ and $a \in A$, $c(x, a)=1$ if $x \notin X_{G}$, and $c(x, a)=0$ otherwise.

Each state of this POMDP is a pair $(s, q)$ indicating the situation where, under an execution of the system, the current state of the event model is $s$ and the current state of the DFA is $q$. For each $x, x^{\prime} \in X$ and $a \in A, \mathbf{T}\left(x, a, x^{\prime}\right)$ gives the probability of transitioning from state $x$ to state $x^{\prime}$ under performance of action $a$. In the context of our event model, each transition corresponds to a situation where the robot chooses an event $e$ to observe and the event model


Fig. 1: a) An event model $\mathcal{M}$ with its observation model $\mathcal{B}$. b) A DFA $\mathcal{D}$, specifying event sequences that contain at least one event. c) The Goal POMDP $\mathcal{P}_{(\mathcal{M}, \mathcal{B} ; \mathcal{D})}$, constructed by Definition 5. (Self-loop transitions of the goal states have been omitted to try reduce visual clutter.)
makes a transition from a state $s$ to $s^{\prime}$. If $e$ appears in $\mathrm{g}\left(s^{\prime}\right)$, then the robot records $e$ and then changes the current state of the DFA to $\delta(q, e)$; otherwise, it does nothing and the DFA remains in state $q$. These correspond to cases (4.a) and (4.b) above, respectively. Case (4.c) makes all the goal states of the POMDP absorbing states. The goal states of the POMDP are those in which the robot has recorded a story, i.e., the current state of the specification DFA is accepting.

For each $a \in A, x \in X$, and $z \in Z$, the function $\mathbf{O}(a, x, z)$ is an observation model, its value being the probability of observing $z$ given that the system has entered state $x$ via action $a$. The POMDP has a special observation, $\perp$, which is observed only when a goal state is reached. Any other observation is a pair $(r, y)$ where $r \in\{$ True, False\} discloses whether the robot's prediction was correctthe event did happen - or not, and $y$ indicates the sensed observation the robot made (as per $\mathcal{B}$ ). Rules $7 \mathrm{a}-7 \mathrm{~d}$ ensure that the first element of the observation pair informs the robot whether its prediction was correct. To see this, if the robot has predicted $e$ to occur, the event model has entered state $s$ such that $e \in g(s)$, and the robot has made an observation $y$, then the probability of observing (True, $y$ ) by entering to state $(s, q)$ via action $e$ is equal $h(s, y)$ (case 7a). If event $e \notin g(s)$, then the robot's prediction has to be wrong, and thus, the probability of observing (False, $y$ ) in state $(s, q)$ when it is reached via action $e$ is $h(s, y)$ (expressed in case 7c). Cases 7b and 7d ensure that there is no misreporting of the correctness of the prediction. Case 7e indicates the observation that the robot has completed recording of a story in $\mathcal{L}(\mathcal{D})$.

Figure 1 illustrates this construction for an elementary example.

### 4.2 Solving the Goal POMDP

A POMDP is usually formulated as a fully observable MDP called a belief MDP whose (continuous) state space consists of the belief space of the POMDP. Accordingly, in the belief MDP from Goal POMDP $\mathcal{P}=\left(X, A, b_{0}, \mathbf{T}, X_{G}, Z, \mathbf{O}, c\right)$, for each belief state $b \in \Delta(X)$, action $a \in A$, and observation $z \in Z$, we denote the updated belief state of $b$ after action $a$ and observation $z$ by $b_{z}^{a}$. It is computed as follows:

$$
\begin{equation*}
b_{z}^{a}(x)=\operatorname{Pr}(x \mid z, a, b)=\frac{\mathbf{O}(a, x, z) \sum_{x^{\prime} \in X} \mathbf{T}\left(x^{\prime}, a, x\right) b(x)}{\operatorname{Pr}(z \mid a, b)} \tag{3}
\end{equation*}
$$

in which,

$$
\begin{equation*}
\operatorname{Pr}(z \mid a, b)=\sum_{x \in X} \mathbf{O}(z, a, x) \sum_{x^{\prime} \in X} \mathbf{T}\left(x^{\prime}, a, x\right) b(x) \tag{4}
\end{equation*}
$$

For this belief MDP, the cost of each action $a$ at belief state $b$ is $c^{\prime}(b, a)=$ $\sum_{x \in X} b(x) c(x, a)$, which in our case, $c^{\prime}(b, a)=1$ if $b$ is a not a goal belief state, and otherwise $c^{\prime}(b, a)=0$. An optimal policy $\pi^{\prime *}: X \rightarrow A$ for this MDP is formulated as a solution to the Bellman recurrences

$$
\begin{gather*}
V^{\prime *}(b)=\min _{a \in A}\left(c^{\prime}(b, a)+\sum_{z \in Z} \operatorname{Pr}(z \mid a, b) V^{\prime *}\left(b_{z}^{a}\right)\right),  \tag{5}\\
\pi^{\prime *}(b)=\underset{a \in A}{\arg \min }\left(c^{\prime}(b, a)+\sum_{z \in Z} \operatorname{Pr}(z \mid a, b) V^{\prime *}\left(b_{z}^{a}\right)\right) . \tag{6}
\end{gather*}
$$

One can use any standard technique to solve these recurrences. For surveys on methods, see $[1,17,20]$. An optimal policy computed via these recurrences prescribes, for any belief state reachable from $b_{0}$, an optimal action to execute. Accordingly, the robot executes at each step, the action given by the optimal policy, and then updates its belief state via (3). One can show, via induction, that at each step $i$, there is a unique $q_{i} \in Q$ such that belief state $b_{i}$ has outcomes only for (but probably not all) $x_{j}=\left(s_{j}, q_{i}\right) \in X, j=1,2, \cdots|S|$. As such, function $\beta: \Delta(X) \rightarrow \Delta(S) \times Q$ maps each $b_{i}$ of those belief states to a tuple $\left(d, q_{i}\right)$, where for each $s \in S, d(s)=b\left(\left(s, q_{i}\right)\right)$. Subsequently, the optimal policy $\pi^{\prime *}$ computed for $\mathcal{P}_{(\mathcal{M}, \mathcal{B} ; \mathcal{D})}$ can be mapped to an optimal solution $\pi^{*}: \Delta(S) \times Q \rightarrow A$ to Rтм, by interpreting $\pi^{*}\left(\beta\left(b_{i}\right)\right)=\pi^{\prime *}\left(b_{i}\right)$, for each reachable belief state $b_{i} \in \Delta(X)$.

### 4.3 Solving RTM/Fom via Goal MDP

The previous construction can be used to solve RTM/FOM too, but, given that the event model fed into Rtm/Fom is fully observable, to improve solution tractability, it is more sensible to construct a Goal MDP. To do so, for the event model and the DFA in Definition 5, the Goal MDP $\mathcal{M}=\left(X, A, b_{0}, \mathbf{T}, X_{G}, c\right)$ embedded in the POMDP $\mathcal{P}$ in that definition is extracted and then an optimal policy for $\mathcal{M}$ is solved. An optimal policy $\pi^{\prime \prime *}$ for the MDP is a function over $X=S \times Q$, which is computed via the Bellman equations

$$
\begin{gather*}
V^{\prime \prime *}(x)=\min _{a \in A}\left(c(x, a)+\sum_{x^{\prime} \in X} V^{\prime \prime *}\left(x^{\prime}\right) \mathbf{T}\left(x, a, x^{\prime}\right)\right),  \tag{7}\\
\pi^{\prime \prime *}(x)=\underset{a \in A}{\arg \min }\left(c(x, a)+\sum_{x^{\prime} \in X} V^{\prime \prime *}\left(x^{\prime}\right) \mathbf{T}\left(x, a, x^{\prime}\right)\right) . \tag{8}
\end{gather*}
$$

These equations may be solved by a variety of methods (see [7, Chp. 10] for a survey). In the evaluation reported below, we use standard value iteration. After computing $\pi^{\prime \prime *}$, for each $x=(s, q) \in X$, we make a belief state $b \in \Delta(S)$ such that $b\left(s^{\prime}\right)=1$ if and only if $s^{\prime}=s$, and then set $\pi^{*}(b, q)=\pi^{\prime \prime *}((s, q))$, where $\pi^{*}$ is an optimal solution to RTM/Fom. Observe that $\pi^{*}$ for RTM/FOM is only computed for finitely many pairs $(b, q)$, those in which $b$ is a single outcome.

## 5 Representation-invariance of expected time

Notice that the event selected by the policy $\pi^{*}$ at each step depends, in part, on the current state of the specification DFA. Because a single regular language may
be represented with a variety of distinct DFAs with different sets of states -and thus, their optimal policies cannot be identical - one might wonder whether the expected execution time achieved by their computed policies depends on the specific DFA, rather than only on the language. The question is particularly relevant in light of the language mutators we examine in Section 6. Here, we show that the expected number of steps required to capture a story within a given event model does indeed depend only on the language specified by the DFA, and not on the particular representation of that language.

For a DFA $\mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$, we define a function $f: Q \rightarrow\{0,1\}$ such that for each $q \in Q, f(q)=1$ if $q \in F$, and otherwise, $f(q)=0$. Now consider the well-known notion of bisimulation, defined as follows:
Definition 6 (bisimulation [18]). Given DFAs $\mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$ and $\mathcal{D}^{\prime}=$ $\left(Q^{\prime}, E, \delta^{\prime}, q_{0}^{\prime}, F^{\prime}\right)$, a relation $R \subseteq Q \times Q^{\prime}$ is a bisimulation relation for $\left(\mathcal{D}, \mathcal{D}^{\prime}\right)$ if for any $\left(q, q^{\prime}\right) \in R$ : (1) $f(q)=f^{\prime}\left(q^{\prime}\right)$; (2) for any $e \in E$, $\left(\delta(q, e), \delta^{\prime}\left(q^{\prime}, e\right)\right) \in R$.
Bisimulation implies language equivalence and vice versa.
Proposition 1. ([18]) For two $D F A s \mathcal{D}=\left(Q, E, \delta, q_{0}, F\right), \mathcal{D}^{\prime}=\left(Q^{\prime}, E, \delta^{\prime}, q_{0}^{\prime}, F^{\prime}\right)$, we have $\mathcal{L}(\mathcal{D})=\mathcal{L}\left(\mathcal{D}^{\prime}\right)$ iff $\left(q_{0}, q_{0}^{\prime}\right) \in R$ for a bisimulation relation $R$ for $\left(\mathcal{D}, \mathcal{D}^{\prime}\right)$.
Bisimulation is preserved for any reachable pairs. The state to which a DFA with transition function $\delta$ reaches by tracking an event sequence $r$ from state $q$ is denoted $\delta^{*}(q, s)$.
Proposition 2. If $\left(q, q^{\prime}\right)$ are related by a bisimulation relation $R$ for $\left(\mathcal{D}, \mathcal{D}^{\prime}\right)$, then for any $r \in E^{*},\left(\delta^{*}(q, r), \delta^{\prime *}\left(q^{\prime}, r\right)\right) \in R$.
We now define a notion of equivalence for a pair of belief states.
Definition 7. Given an event model $\mathcal{M}=\left(S, \mathbf{P}, s_{0}, E, g\right)$, an observation model $\mathcal{B}=(Y, h)$ for $\mathcal{M}, D F A s \mathcal{D}=\left(Q, E, \delta, q_{0}, F\right)$ and $\mathcal{D}^{\prime}=\left(Q^{\prime}, E, \delta^{\prime}, q_{0}^{\prime}, F^{\prime}\right)$ such that $\mathcal{L}(\mathcal{D})=\mathcal{L}\left(\mathcal{D}^{\prime}\right)$, let $\mathcal{P}_{(\mathcal{M}, \mathcal{B} ; \mathcal{D})}=\left(X, A, b_{0}, \mathbf{T}, X_{G}, Z, \mathbf{O}, c\right)$ and $\mathcal{P}_{\left(\mathcal{M}, \mathcal{B} ; \mathcal{D}^{\prime}\right)}^{\prime}=$ $\left(X^{\prime}, A, b_{0}^{\prime}, \mathbf{T}^{\prime}, X_{G}^{\prime}, Z, \mathbf{O}^{\prime}, c^{\prime}\right)$. For two reachable belief states $b \in \Delta(X)$ and $b^{\prime} \in$ $\Delta\left(X^{\prime}\right)$, with $\beta(b)=(d, q)$ and $\beta^{\prime}\left(b^{\prime}\right)=\left(d^{\prime}, q^{\prime}\right)$, we say that $b^{\prime}$ is equivalent to $b$, denoted $b \equiv b^{\prime}$, if (1) $\left(q, q^{\prime}\right)$ are related by a bisimulation relation for $\left(\mathcal{D}, \mathcal{D}^{\prime}\right)$ and that (2) $d=d^{\prime}$, i.e. for each $s \in S, d(s)=d^{\prime}(s)$.
Equivalence is preserved for updated belief states.
Lemma 1. Given the structures in Definition 7, let $b \in \Delta(X)$ and $b^{\prime} \in \Delta\left(X^{\prime}\right)$ be two reachable belief states such that $b \equiv b^{\prime}$. For any action $a \in A$ and observation $z \in Z$, it holds that $b_{z}^{a} \equiv{b^{\prime}}_{z}^{a}$ and that $\operatorname{Pr}(z \mid a, b)=\operatorname{Pr}\left(z \mid a, b^{\prime}\right)$.

Note that for a Goal POMDP $\mathcal{P}$ with initial belief state $b_{0}, V^{*}\left(b_{0}\right)$ is the expected cost of reaching a goal belief state by an optimal policy for $\mathcal{P}$. We now present our result.
Theorem 1. For the structures in Definition 7, it holds that $V^{*}\left(b_{0}\right)=V^{\prime *}\left(b_{0}^{\prime}\right)$.
Proof. For a belief MDP $\mathcal{M}$, let $\operatorname{Tree}(\mathcal{M})$ to be its tree-unravelling-the tree whose paths from the root to the leaf nodes are all possible paths in $\mathcal{M}$ that start from the initial belief state. A policy $\pi$ for $\mathcal{M}$ chooses a fixed set of paths over $\operatorname{Tree}(\mathcal{M})$, and the expected cost of reaching a goal belief state under $\pi$ is
equal to $\sum_{p \in \operatorname{GoalPaths}(\pi, \operatorname{Tree}(\mathcal{M}))} C(p) * W(p)$, where $\operatorname{GoalPaths}(\pi, \operatorname{Tree}(\mathcal{M}))$ is the set of all paths that are chosen by $\pi$ and reach a goal belief state from the root of $\operatorname{Tree}(\mathcal{M}), C(p)$ is the sum of costs of all transitions in path $p$, and $W(p)$ is the product of the probability values of all transitions in $p$. The idea is that if we can overlap the tree-unravellings of the belief MDPs $\mathcal{P}_{(\mathcal{M}, \mathcal{B} ; \mathcal{D})}$ and $\mathcal{P}_{\left(\mathcal{M}, \mathcal{B} ; \mathcal{D}^{\prime}\right)}^{\prime}$ in such a way that each pair of overlapped belief states are equivalent in the sense of Definition 7 and that each pair of overlapped transitions have the same probability and the same cost, then for each pair of overlapped belief states $b \in \Delta(X)$ and $b^{\prime} \in \Delta\left(X^{\prime}\right)$, if we use $\pi^{*}(b)$ as the decision at the belief state $b^{\prime}$, then because those fixed paths are overlapped, then $V^{*}\left(b_{0}\right) \geq V^{* *}\left(b_{0}^{\prime}\right)$. And, in a similar fashion, $V^{*}\left(b_{0}\right) \leq V^{\prime *}\left(b_{0}^{\prime}\right)$, and thus, $V^{*}\left(b_{0}\right)=V^{\prime *}\left(b_{0}^{\prime}\right)$. The following construction makes those trees and shows how we can overlap them.

For an integer $n \geq 1$, we can make two trees $T_{n}$ and $T_{n}^{\prime}$ by the following procedure. (1) Set $b_{0}$ as the root of $T_{n}$ and set $b_{0}^{\prime}$ as the root of $T_{n}^{\prime}$; make a relation $R$ and set $R \leftarrow\left\{\left(b_{0}, b_{0}^{\prime}\right)\right\}$. (2) While $\left|T_{n}\right|<n$, extract a pair $\left(b, b^{\prime}\right)$ from $R$ that has not been checked yet and in which $b$ and $b^{\prime}$ are not goal belief states; for each action $a$ and observation $z$, compute $b_{z}^{a}$ and $b_{z}^{\prime a}$, add node $b_{z}^{a}$ and edge $\left(b, b_{z}^{a}\right)$ to $T$, and add node $b^{\prime}{ }_{z}^{a}$ and edge $\left(b^{\prime}, b_{z}^{\prime a}\right)$ to $T^{\prime}$; label both edges $(a, z)$. Also assign to edge $\left(b, b_{z}^{a}\right), \operatorname{Pr}(z \mid a, b)$ as its probability value, and set the probability value of $\left(b^{\prime}, b_{a}^{\prime z}\right), \operatorname{Pr}\left(z \mid a, b^{\prime}\right)$; the cost of each edge is set 1 .

Given that $\mathcal{L}(\mathcal{D})=\mathcal{L}\left(\mathcal{D}^{\prime}\right)$, by Proposition 1 , states $q_{0}$ and $q_{0}^{\prime}$ are related by a bisimulation relation for $\left(\mathcal{D}, \mathcal{D}^{\prime}\right)$, which by Definition 7 and the construction in Definition 5 implies that $b_{0} \equiv b_{0}^{\prime}$. This combined with Lemma 1 implies that for each pair $\left(b, b^{\prime}\right) \in R, b \equiv b^{\prime}$. We now overlap $T_{n}$ and $T_{n}^{\prime}$ such that each pair $\left(b, b^{\prime}\right)$ that are related by $R$ are overlapped. By Lemma 1, each pair of overlapped edges have the same probability value and the same cost value. Since for any integer $n \geq 0$ we can overlap trees $T_{n}$ and $T_{n}^{\prime}$ in the desired way, we can overlap the tree-unravellings of the belief MDPs of $\mathcal{P}_{(\mathcal{M}, \mathcal{B} ; \mathcal{D})}$ and $\mathcal{P}_{\left(\mathcal{M}, \mathcal{B} ; \mathcal{D}^{\prime}\right)}^{\prime}$ in the desired way too; this completes the proof.

The upshot of this analysis is that we can indeed attend only to the story specification language (given indirectly via $\mathcal{D}$ ) and that the specific presentation of that language does not impact the expected number of steps to capture an event sequence satisfying that specification.

## 6 Construction of Specification Languages

In this section we describe how one might construct, in a partially automated way, specifications for a variety of interesting scenarios. The idea is to use a variety of mutators to construct specification DFAs.

### 6.1 Multiple recipients

Suppose we would like to capture several videos, one for each of several recipients, within a single execution. Given language specifications $\mathcal{D}_{1}, \ldots, \mathcal{D}_{n} \in \mathscr{D}$, where $\mathscr{D}$ denotes the set of all DFAs over a fixed event set $E$, how can we form a
single specification that directs the robot to capture events that can be postprocessed into the individual output sequences? One way is via two relatively simple operations on DFAs:
$\left(\mathbf{M}_{\mathbf{S}}\right)$ A supersequence operation $\mathbf{M}_{\mathbf{S}}: \mathscr{D} \rightarrow \mathscr{D}$, where

$$
\begin{equation*}
\mathcal{L}\left(\mathbf{M}_{\mathbf{S}}(\mathcal{D})\right)=\left\{w \in E^{*} \mid \exists w^{\prime} \in \mathcal{L}(\mathcal{D}), w^{\prime} \text { is a subsequence of } w\right\} \tag{9}
\end{equation*}
$$

This operation is produced by first treating $\mathcal{D}$ as a nondeterministic finite automaton (NFA), then for each event and state, adding a transition labeled by that event from that state to itself, and converting result back into a DFA [13].
$\left(\mathbf{M}_{\mathbf{I}}\right)$ An intersection operation $\mathbf{M}_{\mathbf{I}}: \mathscr{D} \times \mathscr{D} \rightarrow \mathscr{D}$, under which
$\mathcal{L}\left(\mathbf{M}_{\mathbf{I}}\left(\mathcal{D}_{1}, \mathcal{D}_{2}\right)\right)=\mathcal{L}\left(\mathcal{D}_{1}\right) \cap \mathcal{L}\left(\mathcal{D}_{2}\right)$.
Based on these two operations, we can form a specification that asks the robot to capture an event sequence that satisfies all $n$ recipients as follows:

$$
\begin{equation*}
\mathcal{D}=\mathbf{M}_{\mathbf{I}}\left(\mathbf{M}_{\mathbf{I}}\left(\mathbf{M}_{\mathbf{S}}\left(\mathcal{D}_{1}\right), \mathbf{M}_{\mathbf{S}}\left(\mathcal{D}_{2}\right)\right) \ldots, \mathbf{M}_{\mathbf{S}}\left(\mathcal{D}_{n}\right)\right) \tag{10}
\end{equation*}
$$

Then from any $\xi \in \mathcal{L}(\mathcal{D})$, we can produce a $\xi_{i} \in \mathcal{L}\left(\mathcal{D}_{i}\right)$ by discarding (as a post-production step) some events from $\xi$.

### 6.2 Mistakes were made

What should
the robot do if it cannot capture an event sequence that fits its specification $\mathcal{D}$, either because some necessary events did not occur, or because the robot failed to capture them when they did occur? One possibility is to accept some limited deviation between the desired specification and what the robot actually captures.

Let $d: E^{*} \times E^{*} \rightarrow \mathbb{Z}^{+}$denote the Levenshtein distance [9], that is, a distance metric that measures the minimum number of insert, delete, and substitute operations needed to transform one string into another. A mutator that allows a bounded amount of such distance might be:
$\left(\mathbf{M}_{\mathbf{L}}\right)$ A Levenshtein mutator $\mathbf{M}_{\mathbf{L}}: \mathscr{D} \times \mathbb{Z}^{+} \rightarrow \mathscr{D}$ that transforms a DFA $\mathcal{D}$ into one that accepts strings within a given distance from some string in $\mathcal{L}(\mathcal{D})$.

$$
\begin{equation*}
\mathcal{L}\left(\mathbf{M}_{\mathbf{L}}(\mathcal{D}, k)\right)=\left\{\xi \mid \exists \xi^{\prime} \in \mathcal{L}(\mathcal{D}), d\left(\xi, \xi^{\prime}\right) \leq k\right\} . \tag{11}
\end{equation*}
$$

This mutation can be achieved using a Levenshtein automaton construction $[6,19]$. Then, if the robot captures a sequence in $\mathcal{L}\left(\mathbf{M}_{\mathbf{L}}(\mathcal{D}, k)\right)$, it can be converted to a sequence in $\mathcal{L}(\mathcal{D})$ by at most $k$ edits. For example, an insertion edit would perhaps require the undesirable use of alternative 'stock footage', rendering of appropriate footage synthetically, or simply a leap of faith on the part of the viewer. By assigning the costs associated with each edit appropriately in the construction, we can model the relative costs of these kinds of repairs.

### 6.3 At least one good shot

In some scenarios, there are multiple distinct views available of the same basic event. We may consider, therefore, scenarios in which this kind of good/better correspondence is known between two events, and in which the robot should
endeavor to capture, say, at least one better shot from that class. We define a mutator that produces such a DFA:
$\left(\mathbf{M}_{\mathbf{G}}\right)$ An at-least-k-good-shots mutator $\mathbf{M}_{\mathbf{G}}: \mathscr{D} \times E \times E \times \mathbb{Z}^{+} \rightarrow \mathscr{D}$, in which $\mathbf{M}_{\mathbf{G}}\left(\mathcal{D}, e, e^{\prime}, k\right)$ produces a DFA in which $e^{\prime}$ is considered to be a superior version of event $e$, and the resulting DFA accepts strings similar to those in $\mathcal{L}(\mathcal{D})$, but with at least $k$ occurrences of $e$ replaced with $e^{\prime}$.

The construction makes a DFA in which $\mathcal{D}$ has been copied $k+1$ times, each called a level, with the initial state at level 1 and the accepting states at level $k+1$. Most edges remain unchanged, but each edge labeled $e$, at all levels less than $k+1$, is augmented by a corresponding edge labeled $e^{\prime}$ that moves to the next level. This guarantees that $e^{\prime}$ has replaced $e$ at least $k$ times, before any accepting state can be reached.

## 7 Case studies

In this section, we present two examples solved by a Python implementation of our algorithm. For Rtm/Fom we form the Goal MDP, while for Rtm/Fhm and RTM we form a Goal POMDP. To solve the POMDP, we use APPL online (Approximate POMDP Planning Online) toolkit, which implements the DESPOT algorithm [22]—one of the fastest known online solvers. We compare the results for different observability conditions based upon the expected number of steps the system runs until the robot records a desired story under an optimal policy.

### 7.1 Turisti Oulussa

William is a tourist visiting Oulu as shown in Figure 2a. William's family has secretly contracted a robotic videography company to record him seeing the sights, specifically the Kauppahalli $(k)$, the Hupisaaret park ( $h$ ), and either Tietomaa museum $(t)$ or the Oulu Cathedral (c). The robot does not know William's specific plans, but it does know, through some statistics, that a typical tourist moves among those districts according to the event model in Figure 2b.

The desired video is specified using the DFA in Figure 2c. The robot is given other tasks to do aside from recording William, and thus, cannot merely follow William; it must form a strategy that predicts which events to try to capture. We conducted our experiments in three settings: (1) RTm/Fom: the robot always knows the current district in which William is located, perhaps by the help of some static sensors; (2) RTM: when the robot does not know at which district William is currently located but there is a single useful observation, a message sent from a security guard in district $s_{1}$, that informs the robot that William is in district $s_{1}$ whenever he is there; (3) RTM/FHM: the robot receives no direct knowledge about William's location. We computed the optimal policy for RTm/Fom, case (1), using the Goal MDP approach in Section 4.3. According to this policy, the expected number of steps to record under a optimal policy with full observability, a story satisfying the specification, is approximately 35.24. To verify the correctness of the algorithm, we simulated the execution of this policy 1,000 times. In each simulation, William followed a random path through


Fig. 2: a) Districts of Oulu that William is touring. b) An event model describing how a tourist visit those districts. Edges are labeled with transition probabilities. c) A DFA specifying that the captured story must contain events $k$ and $h$ and at least one of $c$ or $t$. d) A histogram showing for a thousand simulations, the distribution of the number of hours (steps) William (system) circulated (ran) until, under the full observability assumption-the RTм/Fом problem - the robot recorded a story specified by the DFA, and a pie chart showing the distribution of recorded sequences in these simulations. e) Histogram and pie chart for 1,000 simulations of the RTм problem where the current state of event model is observable to the robot only when William is in district $s_{1}$. f) Histogram and pie chart for 1,000 simulations of the Rтм/Fнм problem.
the city according to the event model in Figure 2b, and the robot executed the computed policy to capture an event sequence satisfying the specification. The average number of steps to record a satisfactory sequence for those 1,000 simulations was 35.16 , quite close to the expected number of steps. Figure 2d shows results of those simulations in form of a histogram and a pie chart.

For cases (2) and (3), our algorithm constructed a Goal POMDP, as described by Definition 5, and supplied it to APPL to conduct 1,000 simulations. In case (2), Rтм with a useful observation, the average number of steps to record a desired story was 37.15 , while in case (3), RTM/FHM, the average number of steps was 45.32 . Note how a single observation of whether William is in $s_{1}$ helped the robot to record a story considerably faster than when it did not have any state information. Even a stream of quite limited information, if chosen aptly, can be very useful to this kind of robot. The histograms and the pie charts for these two cases are shown in Figure 2e and Figure 2f, respectively. Note the difference between the histograms of those three settings.


Fig. 3: a) The event model for the behavior of a typical person in a party, which has six states: $I_{i}$, the state of arriving; $E_{i}$, the state of being entertaining; $C_{i}$, for consuming coffee; $B_{i}$, for drinking other beverages; $D_{i}$, for dancing; and $S_{i}$, for smoking. b) The histogram of execution times for 500 simulations of the wedding reception example for RTм/Fом c) The histogram of execution times for 500 simulations of the wedding reception example for RTM with only one single observation of whether Chris is currently smoking or not d) The histogram of execution times for 500 simulations of the wedding reception example for Rтм/Fнм

### 7.2 Wedding reception

A videographer robot is asked to produce videos that convey different stories, assembled from unpredictable events at a wedding reception. The wedding guests include Alice, Bob, and Chris, and the events of interest for any of those guests are: arriving at the reception, (i); dancing, (d); drinking coffee, (c); drinking other beverages, (b); smoking, (s); and being entertained, (e). Each guest has their own sense of the events they would like to see captured: Alice is mainly interested in seeing Chris drinking or smoking, but also has plans to share the last dance with Bob; Bob cares for nothing but seeing his own dancing through the evening, but hopes to share the last dance with Alice; Chris does not care to see any events at all, but Chris's children are concerned about his unhealthy habits, and so if Chris is drinking too much coffee or smoking too much, they would like to know. The robot in that scenario is given three parallel objectives. We can formalize those as languages, shown here for compactness as regular expressions: for Alice, $r_{1}=\left(s_{3}+c_{3}\right)^{+} d_{12}$; for Bob, $r_{2}=\left(d_{2}+d_{12}+d_{23}\right)^{+} d_{12}$; and for Chris, $r_{3}=\left(s_{3}+c_{3}\right)\left(s_{3}+c_{3}\right)\left(s_{3}+c_{3}\right)^{+}$. These three requests are encoded using DFAs $\mathcal{D}_{1}, \mathcal{D}_{2}$, and $\mathcal{D}_{3}$, respectively.

The behavior of each guest is modeled by the event model in Figure 3a, in which $\mathbf{P}$ is the transition probability function of the model. The joint behavior of the three guests is modeled by an event model $\mathcal{M}$ obtained as the Cartesian product of the models for the individuals, which has $6^{3}$ states in this example. The joint event model is further enhanced with joint events created from single events. For example, $d_{12}$ is the event in which Alice and Bob dance
together. To form a DFA $\mathcal{D}$ from the given specification DFAs, the robot uses $\mathcal{D}=\mathbf{M}_{\mathbf{I}}\left(\mathbf{M}_{\mathbf{I}}\left(\mathbf{M}_{\mathbf{S}}\left(\mathcal{D}_{1}\right), \mathbf{M}_{\mathbf{S}}\left(\mathcal{D}_{2}\right)\right), \mathbf{M}_{\mathbf{S}}\left(\mathcal{D}_{3}\right)\right)$.

Our implementation for this case study consists of 500 simulations for each of the settings Rtm/Fom, Rtm/Fнм, and Rtm where the only observation is if Chris is currently smoking or not, which could perhaps be sensed through a smart smoke detector. The expected number of steps for an optimal policy for Rtm/Fom is 35.2 , and over the 500 simulations, the average number of steps to record a story was 35.63 , which is very close. The average number for RTM with a single useful observation and Rтм/Fнм were respectively 37.68 and 40.4.

## 8 Conclusions and future work

We have considered the problem of minimizing the expected time to record an event sequence satisfying a set of specifications. This was posed as the problem of computing an optimal policy in an associated Markov decision problem. Our implementation has verified that as the robot's ability to perceive the world increases, the expected number of steps to record a desired story decreases. Future work should consider several extensions. For instance, factoring in the means needed to navigate in order to record an event, hence the objective might minimize some expected cost rather than the expected number of steps. Or the case where a set of events (rather than a single event), each assigned to a single robot, may be predicted. Also the case where the robot is given new specification DFAs to satisfy while recording stories for previous requests, especially where those specification DFAs are prioritized and the prioritization is subject to changes [14], or perhaps the case where the robot needs to learn a new event model to describe the environment owing to failure in predicting events.

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